SIMULATING BISTATIC SCATTER FROM SURFACES COVERED WITH VEGETATION

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Abstract—Many experimental and theoretical studies have shown that the use of active systems for monitoring plant biomass suffers from saturation problems. The possibility of overcoming this limit by considering a bistatic configuration is theoretically analyzed for the case of sunflower fields. An electromagnetic model, already developed and validated on active and passive data, has been modified to yield the bistatic scattering coefficient. To this end, coherent scattering from the soil has been included, which resulted to be the most relevant component of specular scattering. According to model simulations, the specular scattering cross section normalized to area does not exhibit severe saturation effects and shows a better sensitivity to biomass at higher frequencies.

1. INTRODUCTION

Monitoring vegetation biomass is one of the relevant applications that remote sensing could find both in ecology [1] and in agriculture [2]. Major applications include, on one side, forestry inventory and deforestation monitoring, and, on the other, crop monitoring, yield estimates, and harvest control. Both their almost all-weather capability and enhanced spatial resolution make imaging radars apt to these tasks.

A number of radar experiments, including spaceborne and airborne SAR, have been carried out to demonstrate a significant correlation of backscattering at different polarizations and frequencies to tree [3–7] or crop [8–13] biomass. The information contained in amplitude and phase of the radar returns makes the retrieval of the vegetation biomass feasible, in principle, by inverting backscattering data. Esti-
mates have been carried out by implementing a variety of techniques, including multiple regressions [3, 6, 14-17], empirical or theoretical algorithms [12, 18], possibly exploiting coherence [19], and neural networks [20-24]. The reported results are generally promising in view of obtaining quantitative information on the vegetation parameters and, in particular, on its biomass. However, both the experience gained from the various projects and theoretical results seem to indicate that a major limit to the actual use of radar in this field exists, due to the early saturation of its response with respect to plant biomass [11, 25]. Among the remedies to overcome this drawback, the use of stepped algorithms, which estimate primary variates for structural classes of forested areas [18] and of neural networks, which have the potential of fully exploiting the multi-dimensionality of the measurement space [26], have been suggested. Although these retrieval techniques can provide powerful means of extracting the biomass information embedded in multi-frequency multi-polarization measurements, devising radar configurations which by themselves have the potential of yielding a higher sensitivity, can be appropriate. Recently, the possible use of a bistatic radar configuration has been considered and theoretically analyzed with the intent of widening the biomass range over which an appreciable radar dynamics is maintained [27]. Such a technique could use a parasitic SAR system based on a non-co-operative illuminator [28], like, for example, a geostationary transmitter and a geosynchronous receiver, as suggested in [29].

Within the general purpose of retrieving the plant biomass, this contribution discusses the relevant features of bistatic scattering from vegetation, on the basis of a simulation analysis carried out using the fully polarimetric theoretical model developed at Tor Vergata [30, 31]. The case of sunflower plants has been chosen as representative of a large class of vegetation, composed of nearly vertical stalks bearing an upper canopy of stems and planar leaves. The analysis can be readily extended to other types of agricultural crops and forests, by tuning the vegetation parameters and possibly including the appropriate growth models.

The normalized scattering cross sections in the specular direction have been calculated at L- and C-band and compared with the back-scattering coefficients computed for the same canopies. For a deeper understanding of the involved scattering mechanisms, the contributions coming from the various components of the canopy and from the
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underlying soil have been evidentiated and discussed. The linear co-polar \((\sigma_{hh}^0, \sigma_{vv}^0)\) and cross-polarized \((\sigma_{hv}^0)\) cases have been considered in detail, but a fully polarimetric analysis has been carried out too. The enhancement of sensitivity with respect to the monostatic case has been noted and its outcome in terms of predicted improvement in the retrieval of biomass is briefly discussed.

2. THE MODEL

The electromagnetic scattering and emission model for vegetated terrain developed at Tor Vergata University considers the vegetation-soil system as a canopy of discrete lossy scatterers overlying a homogeneous lossy half-space with rough interface. Dielectric elements of simple shape, such as discs and cylinders, are assumed: discs represent planar leaves, while cylinders represent trunks, branches, stems and needles. In order to represent a sunflower field, three main canopy components have been identified, as sketched in fig. 1.

![Figure 1. Sketch of model representation for sunflower crops.](image)

- the top layer, filled by twigs and leaves;
- an intermediate layer containing near vertical cylinders representing stalks;
- the bottom layer, representing soil.

The electromagnetic properties of the lossy scatterers, which model the plant constituents, are described by their extinction cross section and by their bistatic scattering cross section, which is a function of the
incident \((\theta, \phi)\) and scattering \((\theta_s, \phi_s)\) directions represented in fig. 2. These quantities are computed using the proper approximation, according to the object dimension and wavelength under consideration. Once the above indicated quantities are known, the different contributions of the top layer scatterers are combined by means of the Matrix Doubling algorithm, which is also applied to include contributions from the soil. Details about the simulation technique, and about the approximations used to model the electromagnetic behaviour of discs, cylinders and of the soil can be found in [31–33]. In those papers, comparisons with experimental results are also shown, which validate the model both in its active and its passive form.

The bistatic scattering coefficient \(\sigma_{pq}(\theta, \theta_s, \phi, \phi_s)\) is composed of two contributions: an incoherent scattering term \(\sigma_{pq}^{oi}(\theta, \theta_s, \phi, \phi_s)\), and a coherent one \(\sigma_{pq}^{oc}(\theta, \theta_s, \phi, \phi_s)\) (where \(p\) and \(q\) are the polarizations of the scattered and incident waves).

In the monostatic case \((\theta = \theta_s, \phi_s = \phi + \pi)\), the backscattering coefficient of the whole canopy system is:

\[
\sigma_{pq}^{cb}(\theta) = \sigma_{pq}^{cbi}(\theta) + \sigma_{pq}^{obl}(\theta)
\]

The first term includes direct backscatter from the soil, the top layer, and multiple scattering effects between them; the second term represents the soil-stalk specular reflection ("corner effect").
When considering scattering in the specular direction \((\theta = \theta_s, \phi_s = \phi)\), there is no soil-stalk corner effect, but coherent scattering from the soil in the specular direction must be taken into account. Therefore, also in this case the scattering coefficient is made up of two terms:

\[
\sigma_{pq}^{\text{co}}(\theta) = \sigma_{pq}^{\text{osi}}(\theta) + \sigma_{pq}^{\text{osc}}(\theta)
\]

As pointed out in [31] and [32], the scattering properties of the top layer-soil system are described by the Fourier components of a scattering function \(S_{mpq}(\theta, \theta_s)\), where \(m\) is the order of the Fourier components, which represent the dependence on the azimuth angle \(\phi_s - \phi\). The incoherent bistatic scattering coefficient results to be proportional to the sum of the Fourier series:

\[
\sigma_{pq}^{\text{oi}}(\theta, \theta_s, \phi, \phi_s) = \alpha \sum_m S_{mpq}(\theta, \theta_s) \cos(m(\phi_s - \phi))
\]

with \(\alpha\) as a proportionality constant.

In the monostatic case, we have:

\[
\sigma_{pq}^{\text{obi}}(\theta) = \alpha \sum_m S_{mpq}(\theta, \theta) \cos(m\pi)
\]

and

\[
\sigma_{pq}^{\text{obc}}(\theta) = T_{qq}(\theta)\sigma_{spq}^{\text{c}}(\theta)T_{pp}(\theta)
\]

where \(\sigma_{spq}^{\text{c}}\) represents the stalk-ground double bounce contribution which is attenuated by the stalks themselves and by the overlying top layer \((T\) represents the overall transmissivity).

In the specular configuration \(\phi_s - \phi = 0\), so that:

\[
\sigma_{pq}^{\text{osi}}(\theta) = \alpha \sum_m S_{mpq}(\theta, \theta)
\]

while

\[
\sigma_{pq}^{\text{osc}}(\theta) = T_{qq}(\theta, \theta)\sigma_{pq}^{\text{osc}}(\theta, \theta, \phi, \phi)T_{pp}(\theta, \theta)
\]

\(\sigma_{pq}^{\text{osc}}(\theta, \theta, \phi, \phi)\) is the coherent scattering coefficient of the soil, in the specular direction. Also in this case, attenuation by the overlying vegetation is introduced by means of the transmissivity \(T\).

The coherent scattering coefficient \(\sigma_{pq}^{\text{osc}}(\theta, \theta, \phi, \phi)\) has been computed using the expression given in [34], where the soil specular reflection Müller matrix [31] has been inserted in order to get the polarimetric contribution. In [34] the coherent scattering coefficient was shown
to depend not only on surface roughness, but also on the system configuration (pixel dimension and radar height). The simulations carried out in this paper refer to system parameters typical of ERS satellite.

2.1 Model Inputs

The vegetation and soil parameters used to model sunflower bistatic scattering have been mostly derived by ground measurements collected in Tuscany during the MAC Europe 91 campaign. Details are given in [11] and [31].

The top layer parameters are:
- Disc (leaf) thickness: $\delta = 0.025$ cm
- Disc radius: $a_D = 8$ cm
- Inclined cylinder (stem) radius: $a_C = 0.25$ cm
- Inclined cylinder length: $\ell_C = 20$ cm
- Leaf and stem moisture content (by weight): 85%
- Leaf and stem orientation distribution:
  \begin{align*}
  0 < \alpha < 2\pi, \quad p(\alpha) &= 1 \\
  0 < \beta < \pi/2, \quad p(\beta) &= 1 \\
  \gamma &= 0
  \end{align*}

At the higher frequencies, since the effects of bending and corrugation become important, we have subdivided each leaf into several circular discs whose diameter has been put equal to half a wavelength.

The stalk layer parameters are:
- Stalk density: $N_s = 7.9$ m$^{-2}$
- Stalk moisture content (by weight): 90%

The soil parameters are:
- Soil roughness standard deviation: $\sigma_z = 1.25$ cm
- Soil roughness average slope: $m_s = 0.3$
- Volumetric soil moisture: $m_V = 17.5\%$

Computations have been carried out for several values of Plant Water Content PWC (kg/m$^2$), which is a significant crop biomass indicator. Some empirical relationships have been found for the following parameters:
- LAI (Leaf Area Index) = $0.9 \times \text{PWC}$
- Stalk height (cm): $h_s = \begin{cases} 
0.75(60 - 10 \times \text{LAI}) \times \text{LAI} & \text{(LAI < 3)} \\
0.75 \times 30 \times \text{LAI} & \text{(LAI > 3)}
\end{cases}$
- Stalk radius (cm): $a_s = 0.75 + 0.125 \times \text{LAI}$
3. THEORETICAL RESULTS

To illustrate the relevant features and the potential of the bistatic technique in monitoring the biomass of agricultural crops, simulations have been conducted at L (1.2 GHz) and C (5.3 GHz) band for an observation angle of 45°. In fig. 3, the computed scattering cross-section, normalized to area, of the sunflower canopy in the specular direction is reported as a function of the Plant Water Content (PWC). For ease of comparison, in fig. 3 the backscattering coefficient modeled for the same canopy and for the same frequencies, is also reported. These plots show that the biomass dependency of radar backscatter varies as a function of radar wavelength and polarization reaching saturation after a certain biomass level. In general it can be noted that, in the monostatic case, HV polarization is the most sensitive to biomass, and that the saturation point is higher for longer wavelength.

In the bistatic configuration, the co-polar responses show a decreasing trend with increasing PWC, without appreciable saturation effect even at the largest biomass values. Furthermore, a larger dynamic range is also apparent: about 20 dB at L-Band in vertical polarization, becoming more than 40 dB at C-Band. The normalized specular cross section in HV polarization is not reported since its values and trend vs PWC are very close to the backscattering case, being null the theoretical soil coherent component.

To get an insight into the bistatic scattering mechanisms, the various contributions coming from the canopy components are reported in fig. 4. (Note that in these plots a larger ordinate scale has been used, in order to incorporate all contributions). The simulation results in fig. 4 indicate that scattering in the specular direction is dominated by the soil coherent component, since all incoherent contributions are several dB’s lower than total specular scattering. Hence, the sensitivity to biomass is connected to the increasing attenuation by the plant canopy, which reduces the coherent scattering from the soil.

The results reported in fig. 4 refer to L-Band, but analogous considerations apply to C-Band. At higher frequencies, attenuation introduced by vegetation is larger, leading to a steeper curve of $\sigma^{os}$ vs PWC.

Since specular reflection is instrumental to the extraction of biomass information, those effects that quench specularity are detrimental to the proposed technique. The impact of soil roughness on the coherent component increases with frequency: at C-band the specular reflection
is cut down by a height standard deviation higher than about 2 cm, whereas at L-band only a moderate decrease ($\approx 10\,\text{dB}$) of the coherent component can be observed for $\sigma_z$ up to 5 cm. On its side, the extension of the surface that could be monitored from a single location of the satellite pair by exploiting the specular bistatic technique is limited by the degree of specularity of the reflection. Indeed, reflection and incidence angles coincide for a single pixel, while their difference increases when the observed region is moved from the central location.
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Figure 4. Components of the normalized scattering cross-section in the specular direction: VV polarization (left), HH polarization (right). $f = 1.2$ GHz, $\theta = 45^\circ$. Continuous line is the soil coherent scattering component; dotted line is the soil incoherent scattering component; dashed line is the top layer component; double dashed line is the top layer-soil interaction component.

To appreciate the sensitivity of the proposed bistatic approach to the degree of specularity, the incidence angle, and consequently the observation angle, have been moved off $\theta = 45^\circ$. This corresponds to observe a pixel at a distance $L = \frac{H\Delta\theta}{\cos^2\theta}$ from the purely specular one ($H$ is the system altitude, and $\Delta\theta$ is the variation in the incidence angle. A flat earth is assumed). In fig. 6 the bistatic scattering coefficient is reported as a function of PWC for various distances. For L-band bistatic observation from an altitude $H = 800$ km, an appreciable sensitivity to vegetation biomass is maintained up to distances $L \simeq 13$ km (i.e., up to an off-specular angle $\Delta\theta \simeq 0.5^\circ$), thus allowing monitoring a strip 26 km wide. Increasing frequency rapidly degrades the sensitivity of off-specular scattering to vegetation biomass: at C-band the expected width of the observable area, in which sensitivity to PWC up to 3 kg/m$^2$ is still appreciable, reduces to less than 6 km.

Finally, in fig. 7 the polarimetric signature of a sunflower field with a PWC=3.5 kg/m$^2$ has been simulated, both in the bistatic and monostatic configurations. The polarimetric signatures exhibit apparent differences in the two configurations. Some peculiarities of the monostatic case are more evidenced in the bistatic case: like the difference between horizontal and vertical polarization, the difference between co- and cross-polar circular polarizations, and the maximum at linear
Figure 5. Bistatic system in an off-specular configuration. $\theta + \Delta \theta$ is the incidence angle, $L$ is the distance from the pixel observed under perfect specularity.

Figure 6. Normalized scattering cross-section in the off-specular direction: VV polarization (left), HH polarization (right). $f = 1.2$ GHz. Continuous line: specular scattering; dashed line: bistatic scattering from a pixel with $L = 5$ Km; dotted line: scattering from a pixel with $L = 10$ Km; dot-dashed line: scattering from a pixel with $L = 15$ Km.
cross-polarization with $45^\circ$ inclination. These results indicate that bistatic data can add information in polarimetric applications, like for example vegetation classification.

4. CONCLUSIONS

It is now becoming possible to perform radar bistatic measurements by using systems deployed for other purposes, like positioning or broadcasting satellites. The use of non-co-operative radar illuminators would reduce the cost of bistatic operation and would make it more affordable by the remote sensing community. Since the scattering cross-section is
sensitive to the geometry of the measurement system and, in particular, to the incidence and scattering angles, such a radar configuration may have the potential of providing data which, for some applications, have better characteristics with respect to the monostatic case. Here we have considered the problem of plant biomass monitoring, which suffers from the early saturation of the backscattering coefficients. To this end, the performance of a bistatic radar in a specular configuration has been simulated to investigate its expected capability of widening the range of biomass over which significant measures can be taken. A numerical model simulating the bistatic normalized scattering section of a sunflower crop has been run and the results have been compared with those obtained for the same canopy in the monostatic case. The most important differences are essentially due to the specular coherent reflection from the soil, which appears to be the dominant component in the scattering process. Hence, the attenuation by the vegetation becomes the main mechanism through which the bistatic radar response depends on the biomass. The reported results indicate that such a bistatic system would maintain an appreciable sensitivity to the PWC of crops over a considerably wider range than in the monostatic operation. From this point of view, C-band would be preferable to L-band, whose attenuation is considerably less sensitive to agricultural vegetation. Similar results can be found for forests, however, it should be pointed out that the roughness of a forest floor is frequently sufficiently high to substantially reduce the specular component. Moreover, a growth model of a natural pine stand [35] points out a decrease of the number of trees per unit area with increasing woody biomass. As shown by our simulations (results not reported here), this ends up in a weaker dependence of the attenuation and, in turn, of the measured scattering, on the biomass. Hence, the advantage that a bistatic configuration could offer over the monostatic one is expected to become less distinct in case of forests, at least for some types of natural stands.

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