

$$\mu_1 = \mu_2 = \mu_0, \epsilon_1'' = \epsilon_2'' = g_1 = g_2 = 0$$

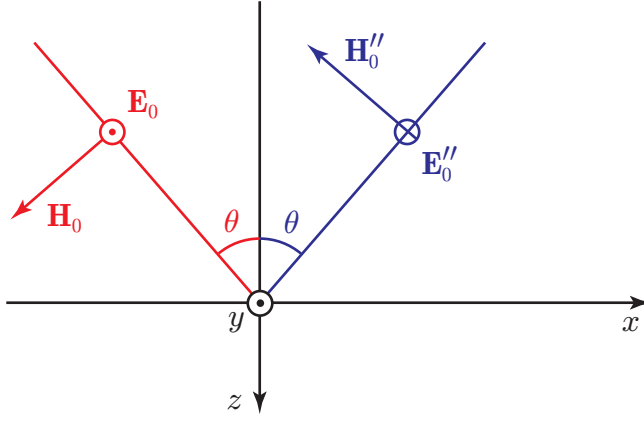
$$\mathbf{E}(\mathbf{r}) = E_0 e^{-j\beta(\sin\theta x + \cos\theta z)} \mathbf{y}_0$$

$$\mathbf{E}''(\mathbf{r}) = q_{Eh} E_0 e^{-j\beta(\sin\theta x - \cos\theta z)} \mathbf{y}_0$$

$$\mathbf{E}_{tot}(\mathbf{r}) = E_0 e^{-j\beta \sin\theta x} (e^{-j\beta \cos\theta z} + q_{Eh} e^{+j\beta \cos\theta z}) \mathbf{y}_0$$

$$= E_0 e^{-j\beta \sin\theta x} (e^{-j\beta \cos\theta z} + q_{Eh} e^{-j\beta \cos\theta z} - q_{Eh} e^{-j\beta \cos\theta z} + q_{Eh} e^{+j\beta \cos\theta z}) \mathbf{y}_0$$

$$= E_0 e^{-j\beta \sin\theta x} \underbrace{[(1 + q_{Eh})]}_{t_{Eh}} e^{-j\beta \cos\theta z} + j 2 q_{Eh} \sin(\beta \cos\theta z) \mathbf{y}_0$$



$$\epsilon_1 = \epsilon_0, \mu_1 = \mu_0, g_1 = 0; \quad g_2 = \infty$$

$$\mathbf{E}(\mathbf{r}) = E_0 e^{-j\beta(\sin\theta x + \cos\theta z)} \mathbf{y}_0$$

$$\mathbf{E}''(\mathbf{r}) = -E_0 e^{-j\beta(\sin\theta x - \cos\theta z)} \mathbf{y}_0$$

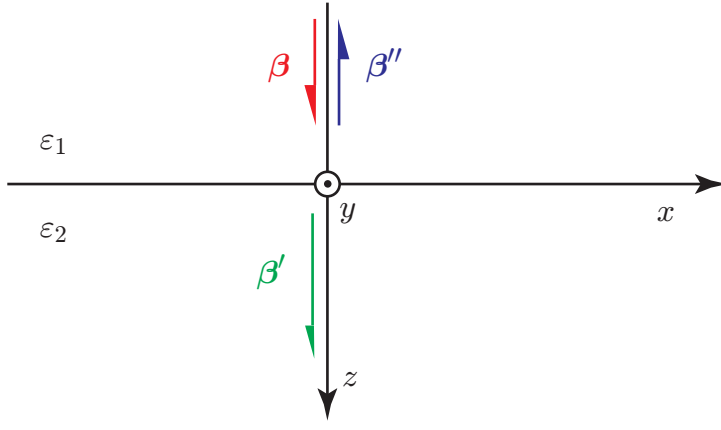
$$\begin{aligned} \mathbf{E}_{\text{tot}}(\mathbf{r}) &= E_0 e^{-j\beta \sin\theta x} (e^{-j\beta \cos\theta z} - e^{j\beta \cos\theta z}) \mathbf{y}_0 \\ &= -2j E_0 e^{-j\beta \sin\theta x} \sin(\beta \cos\theta z) \mathbf{y}_0 \end{aligned}$$

$$\mathbf{H}(\mathbf{r}) = \frac{E_0}{\eta_0} e^{-j\beta(\sin\theta x + \cos\theta z)} (-\mathbf{x}_0 \cos\theta + \mathbf{z}_0 \sin\theta)$$

$$\mathbf{H}''(\mathbf{r}) = \frac{E_0}{\eta_0} e^{-j\beta(\sin\theta x - \cos\theta z)} (-\mathbf{x}_0 \cos\theta - \mathbf{z}_0 \sin\theta)$$

$$\begin{aligned} \mathbf{H}_{\text{tot}}(\mathbf{r}) &= \frac{E_0}{\eta_0} e^{-j\beta \sin\theta x} [e^{-j\beta \cos\theta z} (-\mathbf{x}_0 \cos\theta + \mathbf{z}_0 \sin\theta) \\ &\quad + e^{j\beta \cos\theta z} (-\mathbf{x}_0 \cos\theta - \mathbf{z}_0 \sin\theta)] \\ &= \frac{E_0}{\eta_0} e^{-j\beta \sin\theta x} [- (e^{j\beta \cos\theta z} + e^{-j\beta \cos\theta z}) \mathbf{x}_0 \cos\theta \\ &\quad - (e^{j\beta \cos\theta z} - e^{-j\beta \cos\theta z}) \mathbf{z}_0 \sin\theta] \\ &= 2 \frac{E_0}{\eta_0} e^{-j\beta \sin\theta x} [-\cos(\beta \cos\theta z) \mathbf{x}_0 \cos\theta - j \sin(\beta \cos\theta z) \mathbf{z}_0 \sin\theta] \end{aligned}$$

$$\begin{aligned} \mathcal{P}_{\text{tot}} &= \frac{1}{2} \mathbf{E}_{\text{tot}} \times \mathbf{H}_{\text{tot}}^* \\ &= -2j \frac{|E_0|^2}{\eta_0} \sin(\beta \cos\theta z) [-\cos(\beta \cos\theta z) \overbrace{(\mathbf{y}_0 \times \mathbf{x}_0)}^{-\mathbf{z}_0} \cos\theta \\ &\quad + j \sin(\beta \cos\theta z) \underbrace{(\mathbf{y}_0 \times \mathbf{z}_0)}_{\mathbf{x}_0} \sin\theta] \\ &= 2 \frac{|E_0|^2}{\eta_0} [\sin^2(\beta \cos\theta z) \mathbf{x}_0 \sin\theta - j \sin(\beta \cos\theta z) \cos(\beta \cos\theta z) \mathbf{z}_0 \cos\theta] \\ &= \frac{|E_0|^2}{\eta_0} \{ [1 - \cos(2\beta \cos\theta z)] \mathbf{x}_0 \sin\theta - j \sin(2\beta \cos\theta z) \mathbf{z}_0 \cos\theta \} \end{aligned}$$



$$\mu_1 = \mu_2 = \mu_0, \quad \epsilon_1'' = \epsilon_2'' = g_1 = g_2 = 0$$

$$\mathbf{E}(\mathbf{r}) = E_0 e^{-j\beta z} \mathbf{y}_0$$

$$\mathbf{E}''(\mathbf{r}) = q_E E_0 e^{j\beta z} \mathbf{y}_0$$

$$\begin{aligned} \mathbf{E}_{\text{tot}}(\mathbf{r}) &= E_0 (e^{-j\beta z} + q_E e^{j\beta z}) \mathbf{y}_0 \\ &= E_0 (e^{-j\beta z} + q_E e^{-j\beta z} - q_E e^{-j\beta z} + q_E e^{j\beta z}) \mathbf{y}_0 \\ &= E_0 [(1 + q_E)e^{-j\beta z} + 2j q_E \sin(\beta z)] \mathbf{y}_0 \end{aligned}$$

$$\mathbf{H}(\mathbf{r}) = -\frac{E_0}{\eta_1} e^{-j\beta z} \mathbf{x}_0$$

$$\mathbf{H}''(\mathbf{r}) = q_E \frac{E_0}{\eta_1} e^{j\beta z} \mathbf{x}_0$$

$$\begin{aligned} \mathbf{H}_{\text{tot}}(\mathbf{r}) &= -\frac{E_0}{\eta_1} (e^{-j\beta z} - q_E e^{j\beta z}) \mathbf{x}_0 \\ &= -\frac{E_0}{\eta_1} (e^{-j\beta z} - q_E e^{-j\beta z} + q_E e^{-j\beta z} - q_E e^{j\beta z}) \mathbf{x}_0 \\ &= -\frac{E_0}{\eta_1} [(1 - q_E)e^{-j\beta z} - 2j q_E \sin(\beta z)] \mathbf{x}_0 \end{aligned}$$

$$\begin{aligned} \mathcal{P}_{\text{tot}} = \frac{1}{2} \mathbf{E}_{\text{tot}} \times \mathbf{H}_{\text{tot}}^* &= -\frac{|E_0|^2}{2\eta_1} (e^{-j\beta z} + q_E e^{j\beta z}) (e^{j\beta z} - q_E e^{-j\beta z}) \overbrace{(\mathbf{y}_0 \times \mathbf{x}_0)}^{-\mathbf{z}_0} \\ &= \frac{|E_0|^2}{2\eta_1} (1 - q_E e^{-2j\beta z} + q_E e^{2j\beta z} - q_E^2) \mathbf{z}_0 \\ &= \frac{|E_0|^2}{2\eta_1} [(1 - q_E^2) + 2j q_E \sin(2\beta z)] \mathbf{z}_0 \end{aligned}$$

$$\mathbf{E}'(\mathbf{r}) = (1 + q_E) E_0 e^{-j\beta' z} \mathbf{y}_0$$

$$\mathbf{H}'(\mathbf{r}) = -(1 - q_E) \frac{E_0}{\eta_1} e^{-j\beta' z} \mathbf{x}_0$$

$$\begin{aligned} \mathcal{P}' = \frac{1}{2} \mathbf{E}' \times \mathbf{H}'^* &= -(1 + q_E)(1 - q_E) \frac{|E_0|^2}{2\eta_1} (\mathbf{y}_0 \times \mathbf{x}_0) \\ &= (1 - q_E^2) \frac{|E_0|^2}{2\eta_1} \mathbf{z}_0 \end{aligned}$$